

The power of *Mathematica*

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Along this talk I briefly present my introductory book on *Mathematica*. Its content follows.

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