

## Bounds for the second Hankel determinant of certain bi-univalent functions

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In the present work, we propose to investigate the second Hankel determinant inequalities for certain class of analytic and bi-univalent functions. Some interesting applications of the results presented here are also discussed.

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